

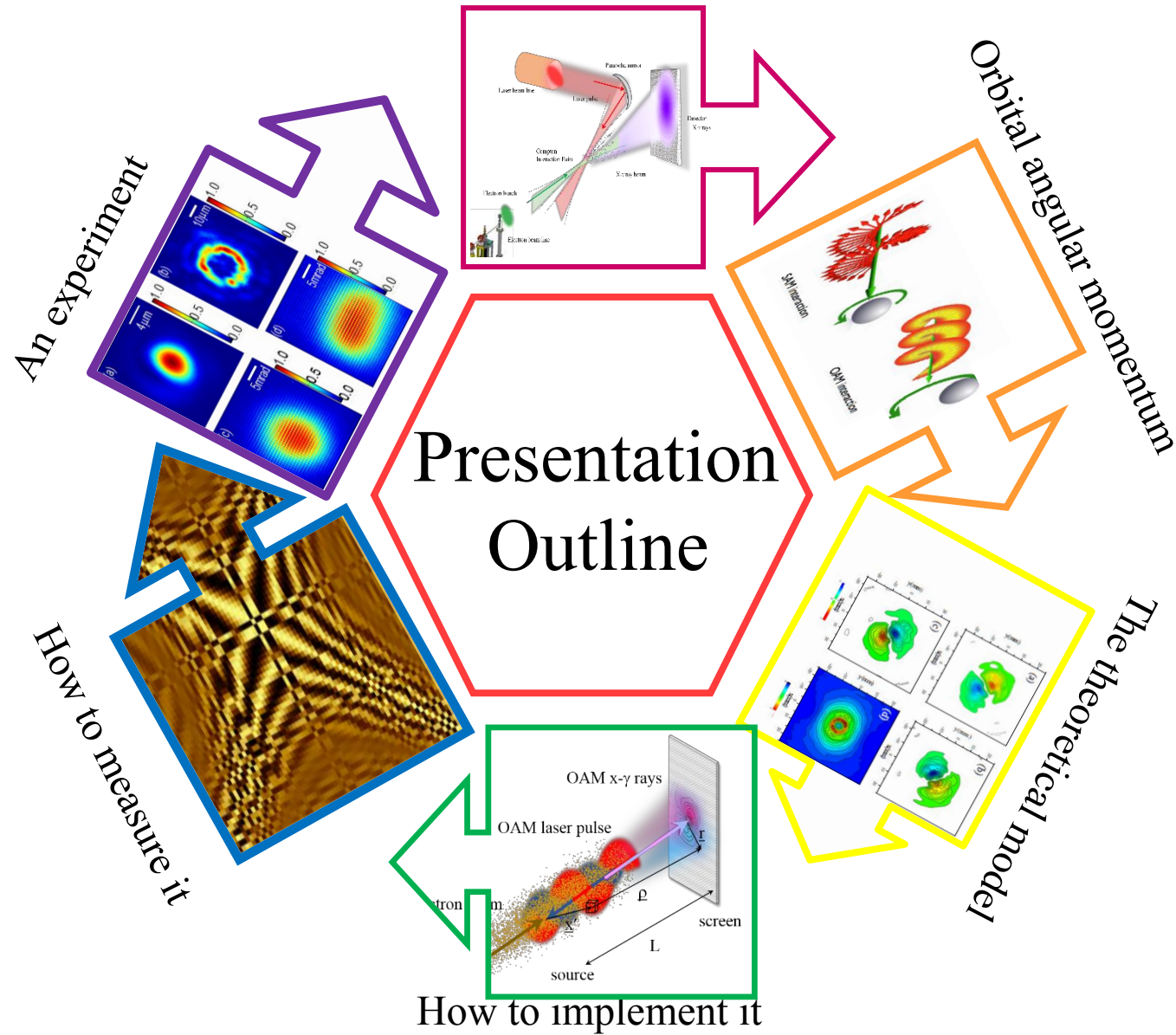
Compton sources with orbital angular momentum

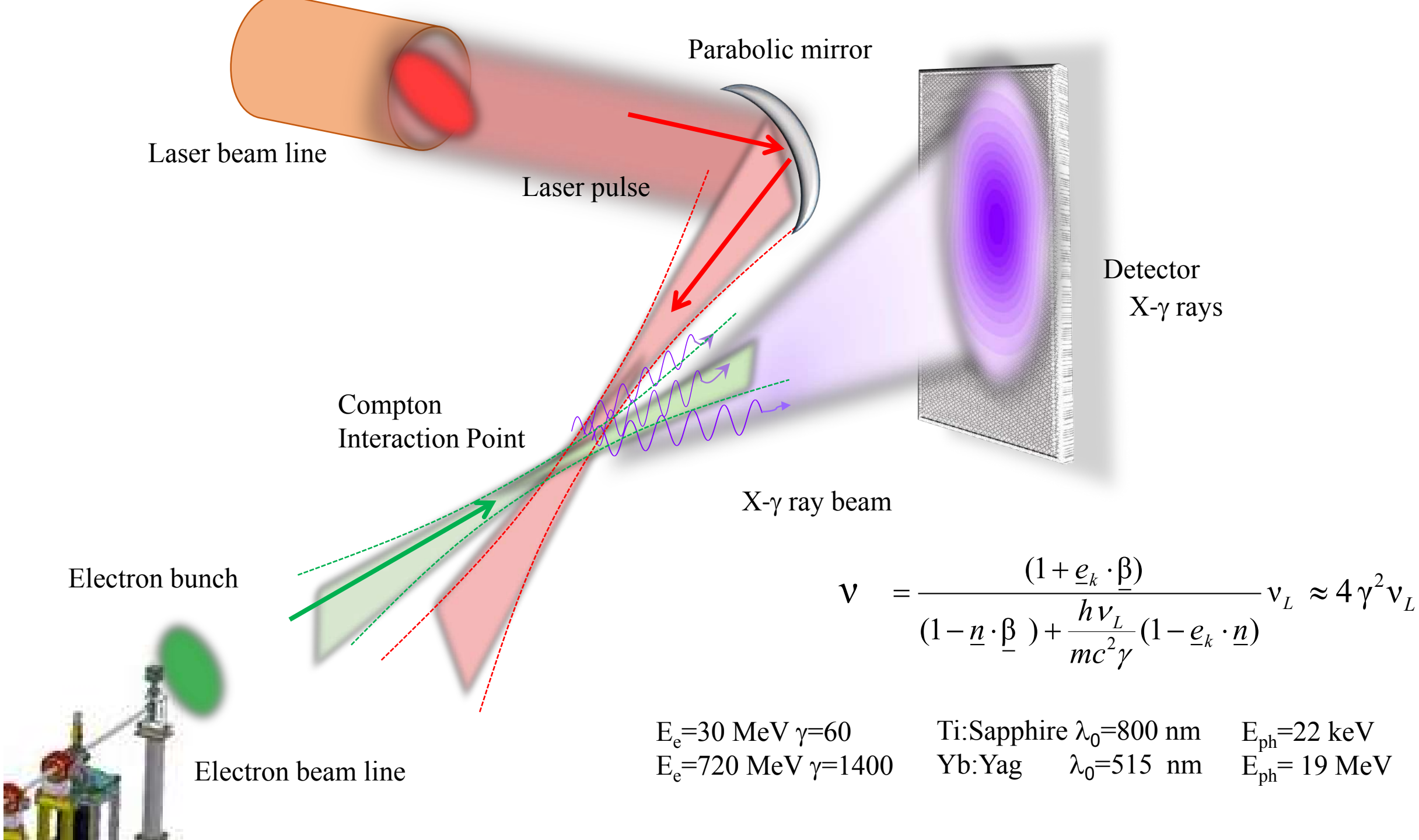
V. Petrillo, I. Drebot, L. Serafini
B. Paroli, M. Siano, A. Cirella, M. Potenza

Thanks to: C. Maroli, A. Bacci, C. Vaccarezza, A. Rossi, C. Curatolo, M. Rossetti, P. Dattoli

and also to all the  and ELI-NP groups

Introduction on Compton scattering





Generalities on Compton scattering, frequency-angle correlation

Compton radiation is frequency-angle correlated

Frequency of the radiation in a direction \underline{n}

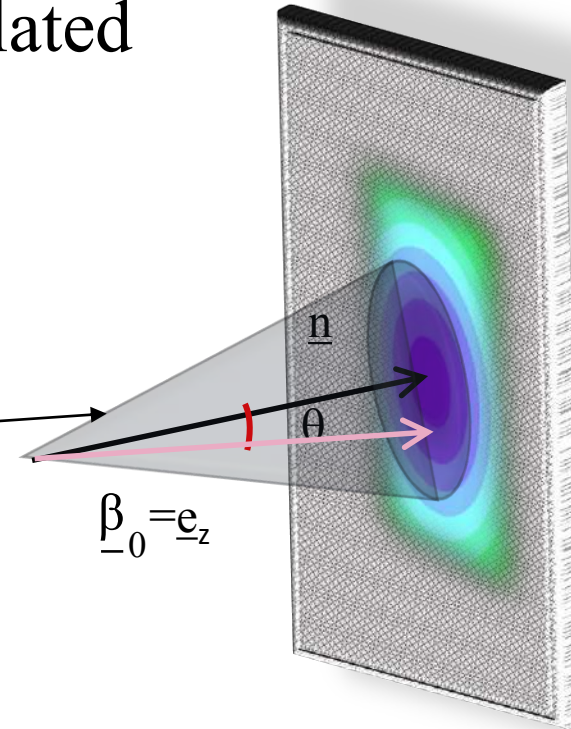
$$\nu = \nu_L \frac{1 - \underline{e}_k \cdot \underline{\beta}_{-0}}{1 - \underline{n} \cdot \underline{\beta}_{-0}} \approx 4\gamma_0^2 \nu_L$$

\swarrow
 $1 - \beta \cos \theta$

Total acceptance

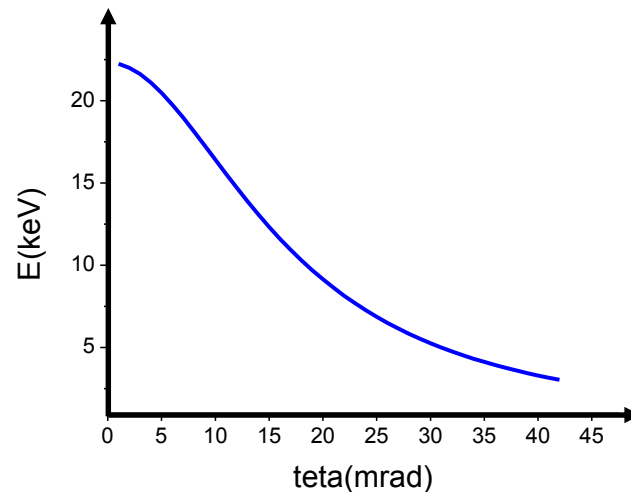
$$\Psi_{\max} = \gamma \theta_{\max} = 1$$

$$\theta_{\max} = 1/\gamma$$



Higher frequencies close to axis

Lower frequencies in the outer part



Frequency-angle correlation

PRL **111**, 114803 (2013) week ending
13 SEPTEMBER 2013

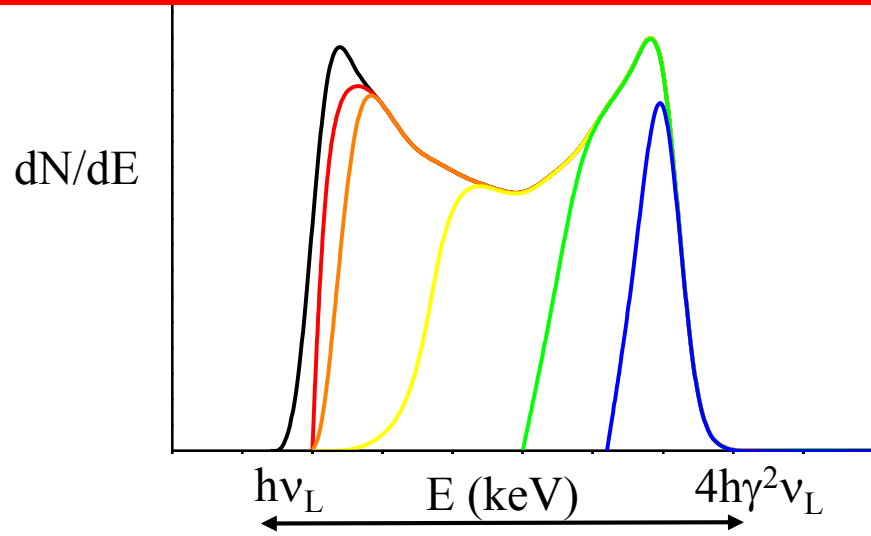
High Resolution Energy-Angle Correlation Measurement of Hard X Rays from Laser-Thomson Backscattering

A. Joehmann,^{1,2,*} A. Irman,¹ M. Bassmann,¹ J. P. Couperus,^{1,2} T. E. Cowan,^{1,2} A. D. Debus,¹ M. Kuntzsch,^{1,2} K. W. D. Ledingham,³ U. Lehnert,¹ R. Sauerbrey,^{1,2} H. P. Schliervoigt,¹ D. Seipt,^{1,2} Th. Stöhler,^{4,5} D. B. Thom,⁴ S. Trotsenko,^{1,2,5} A. Wagner,¹ and U. Schramm¹

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(Received 6 May 2013; published 13 September 2013)

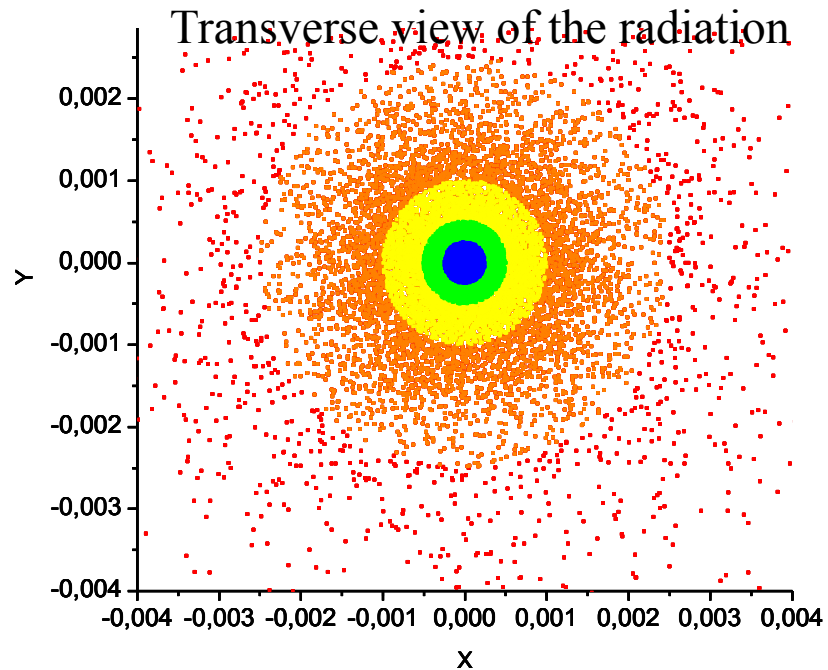
Generalities on Compton scattering, collimation



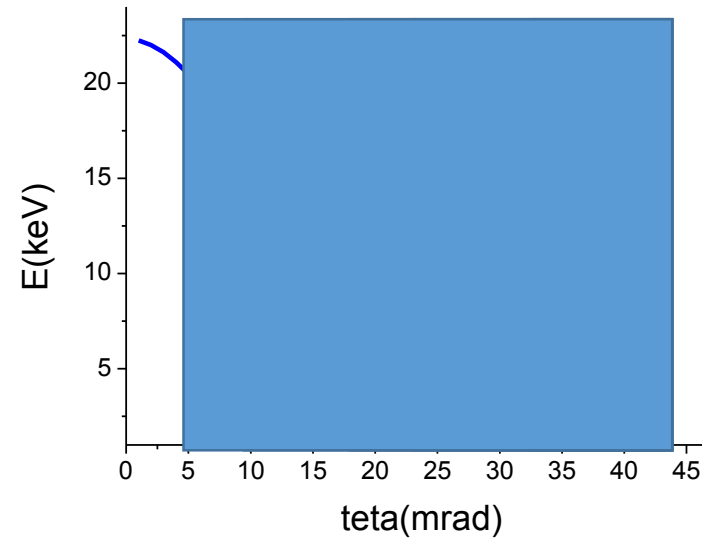
Large natural spectrum

The energy-angle correlation permits the control of bandwidth and divergence

By introducing irides or collimators one can diminish the bandwidth, by selecting the photons close to the axis



Effect of the collimator



Generalities on Compton scattering, polarization

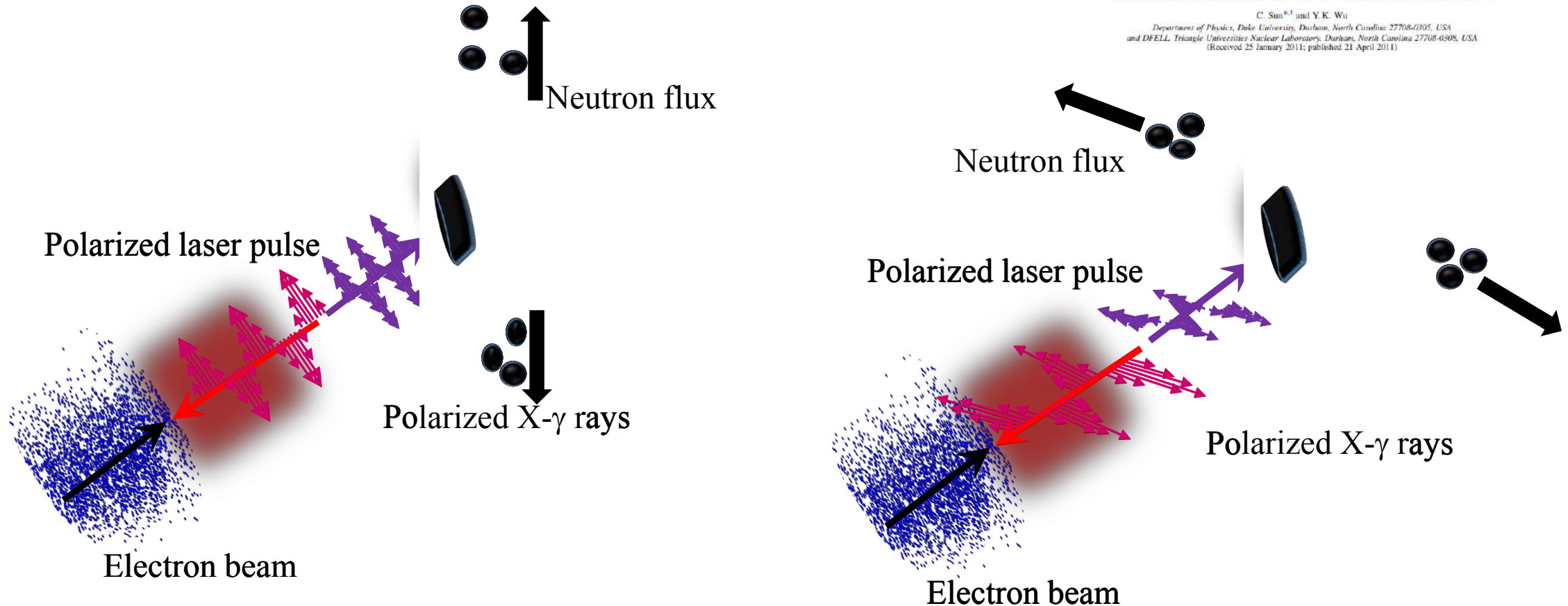
In nuclear photonics experiments, the kinematics of neutrons is strongly influenced by the polarization of the gamma rays

PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS 14, 044701 (2011)

Theoretical and simulation studies of characteristics of a Compton light source

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(Received 25 January 2011; published 21 April 2011)*



Polarization: ELI-NP case

PHYSICAL REVIEW SPECIAL TOPICS—ACCELERATORS AND BEAMS 18, 110701 (2015)

Polarization of x-gamma radiation produced by a Thomson and Compton inverse scattering

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 L. Serafini,² P. Tomasini,¹ C. Vaccarezza,² and A. Variola¹
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 and INFN-Roma1, Piazzale Aldo Moro, 2 00161 Roma, Italy
 (Received 24 June 2015; published 19 November 2015)

ELI-NP Parameters

$E=234\text{-}529$ MeV

$Q=250$ pC

$\varepsilon=0.5$ mm mrad

$\Delta E/E=7 \cdot 10^{-4}$

$\lambda=520$ nm

$E_L=0.2\text{-}0.4$ J

$\delta=8^\circ$

$w_0=28$ μm

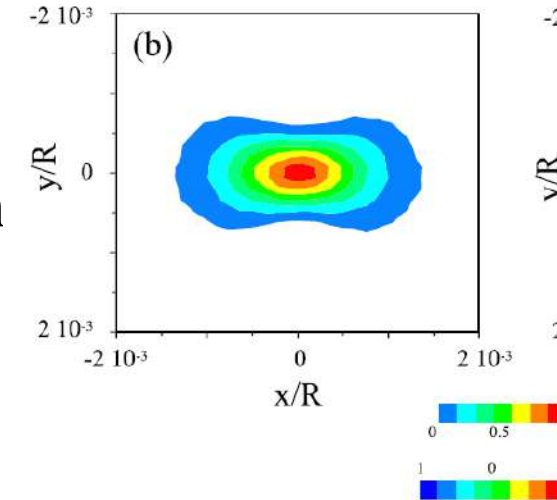
$E_{\text{ph}}=2\text{-}10$ MeV

Total intensity I
 on the screen at 1 m
 $E_{\text{ph}}=10$ MeV

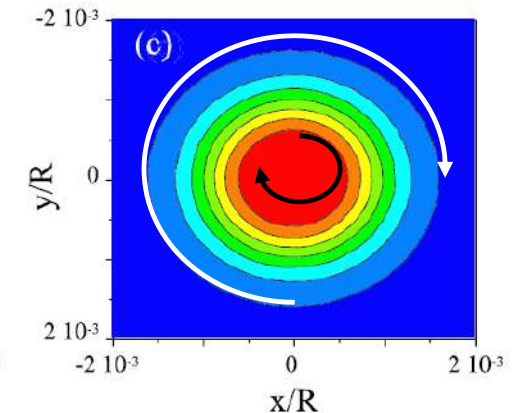
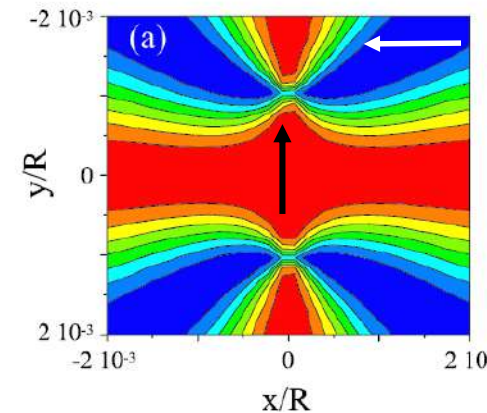
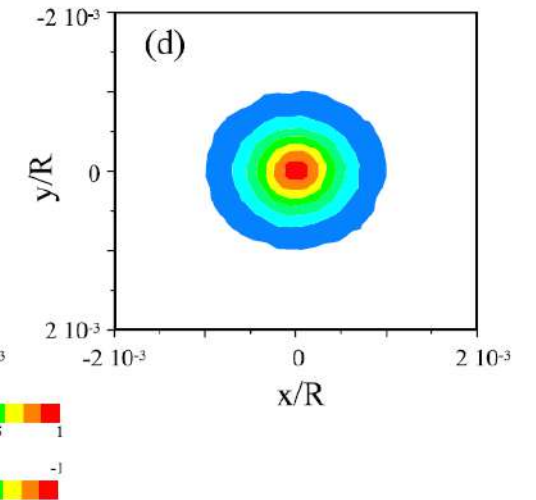
Stokes parameter

$$\frac{(|E_x|^2 - |E_y|^2)}{(|E_x|^2 + |E_y|^2)}$$

Linear polarization
 of the laser \uparrow

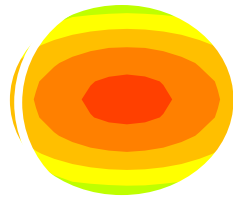


Circular polarization
 of the laser \curvearrowright



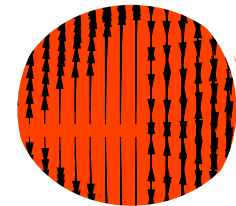
Polarization: ELI-NP case

With a **linear polarization** of the laser:



Total intensity

on the screen at 1 m,
the circle is $1/\gamma$



Stokes parameter

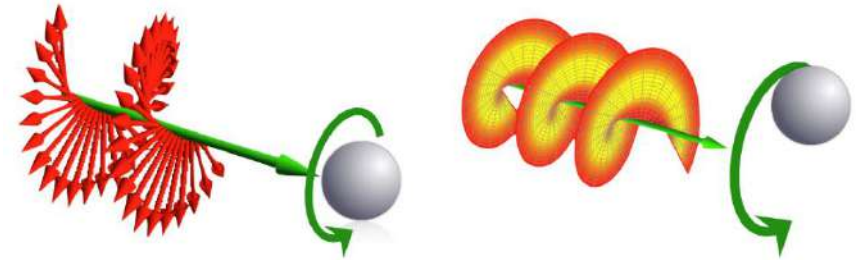
$$(|E_x|^2 - |E_y|^2) / (|E_x|^2 + |E_y|^2)$$

Orbital Angular Momentum (OAM)

Why studying radiation with orbital angular momentum?

Additional degree of freedom

In exp. of photoinization forbidden decays can be excited, molecules in rotational states can resonate in vortex, dipolar and quadrupolar transition can be distinguished.



Spin Ang Mom interaction

Orb Ang Mom interaction

$$s = \frac{1}{2}\hbar$$

$$j = s + m\hbar$$

Pilot experiment with FEL in infrared

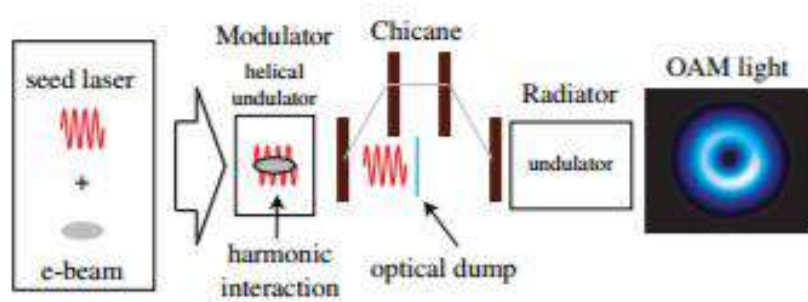


FIG. 1 (color online). Arrangement for generating OAM light in an FEL.

Hemsing, E.; Dunning, M.; Hast, C.; Raubenheimer, T.; Xiang, D. First Characterization of Coherent Optical Vortices from Harmonic Undulator Radiation. *Phys. Rev. Lett.* **2014**, 113, 134803.

How to approach the X/gamma range?

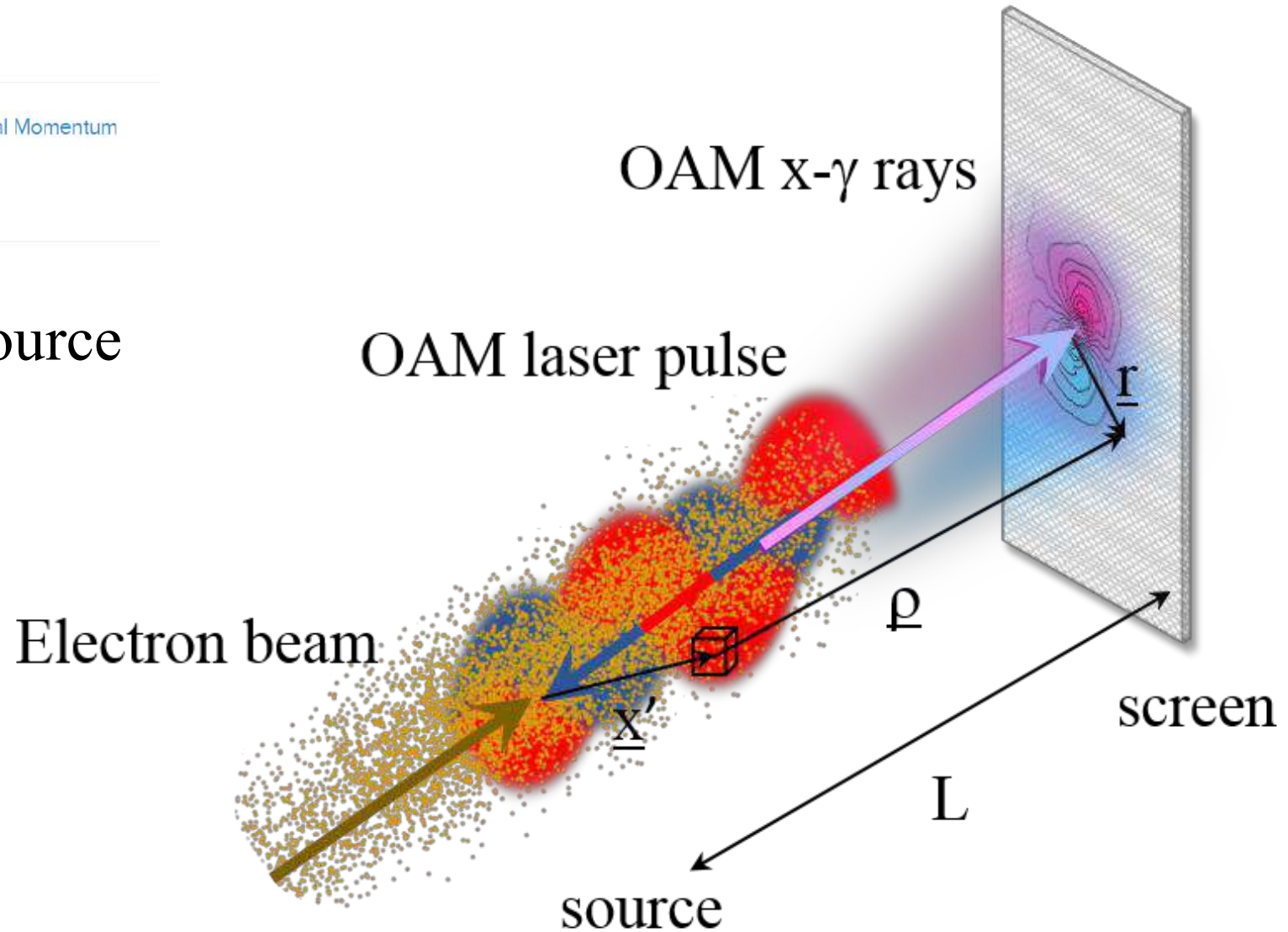
Proposals for OAM X-beams are based on manipulation of electrons in FEL emission. The electrons are treated in such a way that they carry OAM and transfer it to the radiation.

Orbital Angular Momentum (OAM), scheme of the source

Compton Scattered X-Gamma Rays with Orbital Momentum

V. Petrillo, G. Dattoli, I. Drebot, and F. Nguyen
Phys. Rev. Lett. **117**, 123903 (2016) – Published 16 September 2016
[Show Abstract](#)

Scheme of the source



‘Wild type’ electron beam generated by linac

Orbital Angular Momentum, laser structure

Expression and propagation of an OAM laser mode

L. Allen, M. W. Beijersbergen, R. J. C. Spreeuw, and J. P. Woerdman, Phys. Rev. A **45**, 8185 (1992).

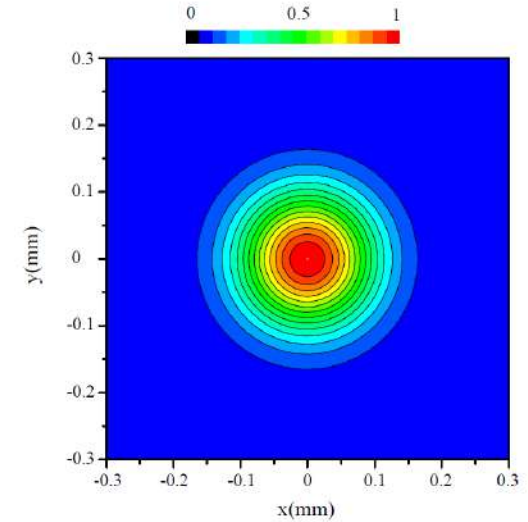
$$\bar{E}_L(x, y, z, t) = \underline{e}_y f(z + ct) E_m(x, y, z) e^{i(\omega t + k_z z)} \quad E_m(x, y, z) = \pi \left(\frac{w_0}{w_z} \right)^2 H_m(\xi, \alpha) e^{-\frac{x^2 + y^2}{2w_z^2}}$$

$$H_m(\xi, \alpha) = m! \sum_{r=0}^{\lfloor m/2 \rfloor} \frac{\alpha^r \xi^{m-2r}}{r!(m-2r)!}$$

$$\xi = \frac{1}{w_0} \left[\left(\frac{w_0}{w_z} \right)^2 (x + i\epsilon y) - (x_0 + i\epsilon y_0) \right]$$

$$\alpha = \frac{i}{2} (1 - \epsilon^2) \frac{\lambda z}{w_z^2}$$

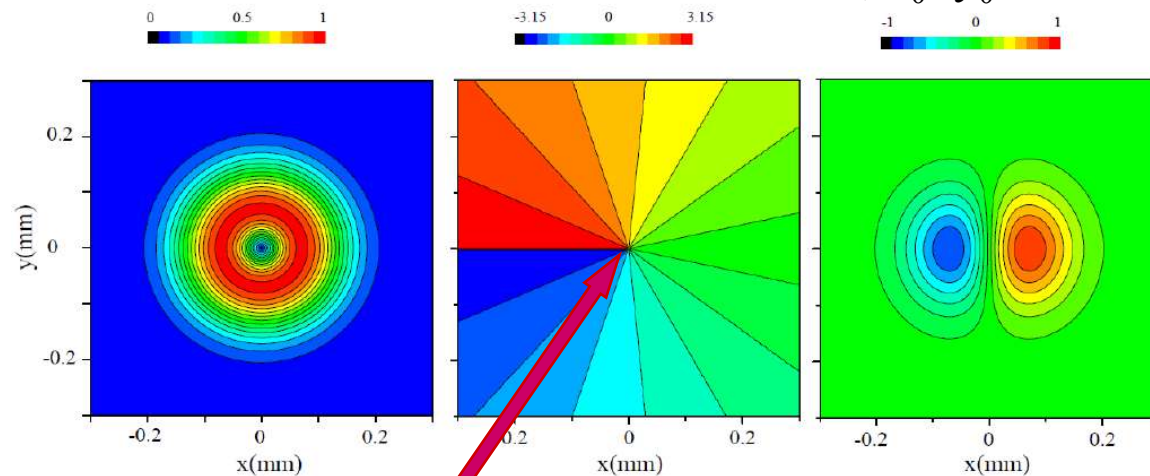
OAM laser modes are generated with fork holograms or phase masks



Gaussian mode

Transverse shape of a laser with OAM, intensity, phase and real part

$m=1, x_0=y_0=0$



vortex

Orbital Angular Momentum, laser structure

Spiral phase plate
 This is the most direct way to generate OAM. A glass plate with a refractive index n and azimuthally varying thickness changes the optical path length, generating the characteristic twisted phasefront.

$\frac{t\lambda}{n-1}$

$\pi/2$ converter
 This method converts a diagonally aligned Hermite-Gauss mode into a Laguerre-Gauss mode by introducing a Gouy phase shift between the vertical and horizontal direction using two cylindrical lenses.

$\sqrt{2}f$

$\frac{1}{\sqrt{2}} HG_{10} + HG_{01}$ $\frac{1}{\sqrt{2}} HG_{10} + i HG_{01}$

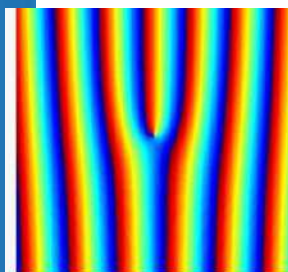
LG_0^1

Spatial light modulator (SLM)
 The most convenient method today is based on digital holograms displayed on an SLM. This allows generation of light with arbitrary phase and amplitude, including OAM beams and their superpositions.

Digital hologram

Optical 'ferris wheel'

$\frac{1}{\sqrt{2}} LG_0^1 + \sqrt{\frac{11}{5}} LG_1^1$



OAM laser modes are generated with fork holograms or phase masks

Porro prism resonator
 Two Porro prisms, forming the end mirrors of a laser cavity, produce superpositions of positive and negative OAM modes where the mode order is dictated by the relative orientation of the two prisms.

$=$ $+$

Q-plate
 In a Q-plate, the optical axes of liquid crystals are rotated with respect to the center of the device. This couples the spin and orbital parts of light's angular momentum, resulting in the generation of OAM.

$q=2$

Left circular polarization

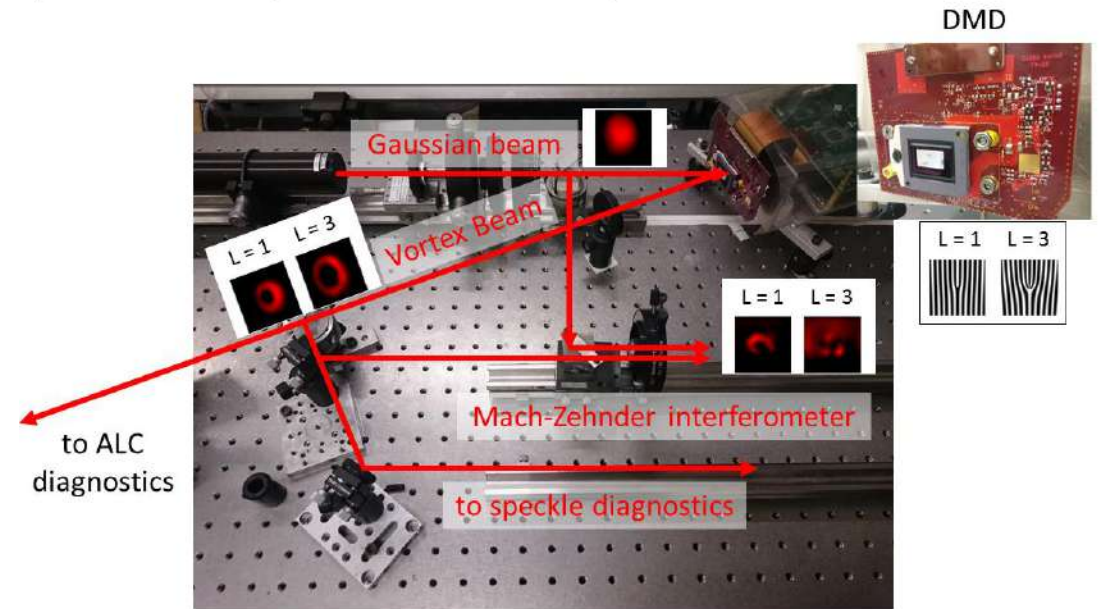
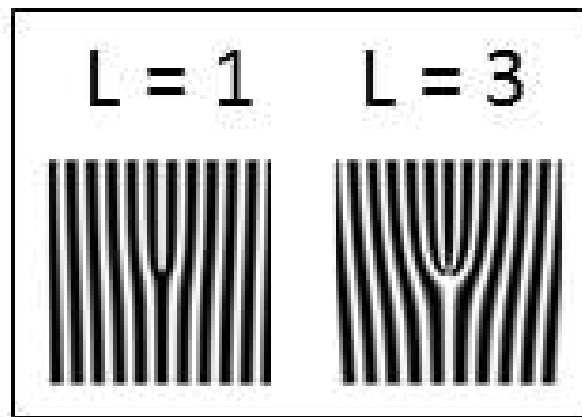
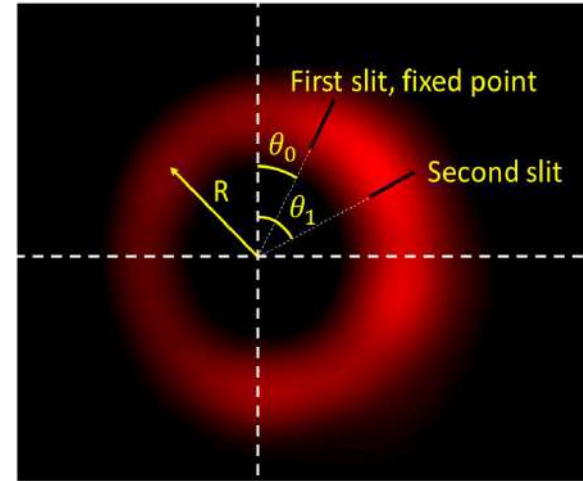
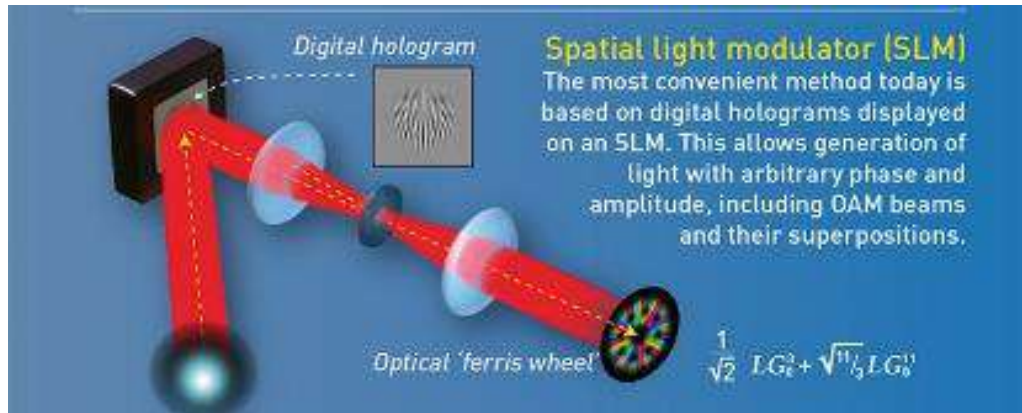
Right circular polarization

Fresnel cone
 Reflection from a conical geometry produces OAM through acquisition of a geometric phase. In addition, glass cones use phase shifts arising from Fresnel's equations to shape the polarization.

Polarization profile

Phase profile

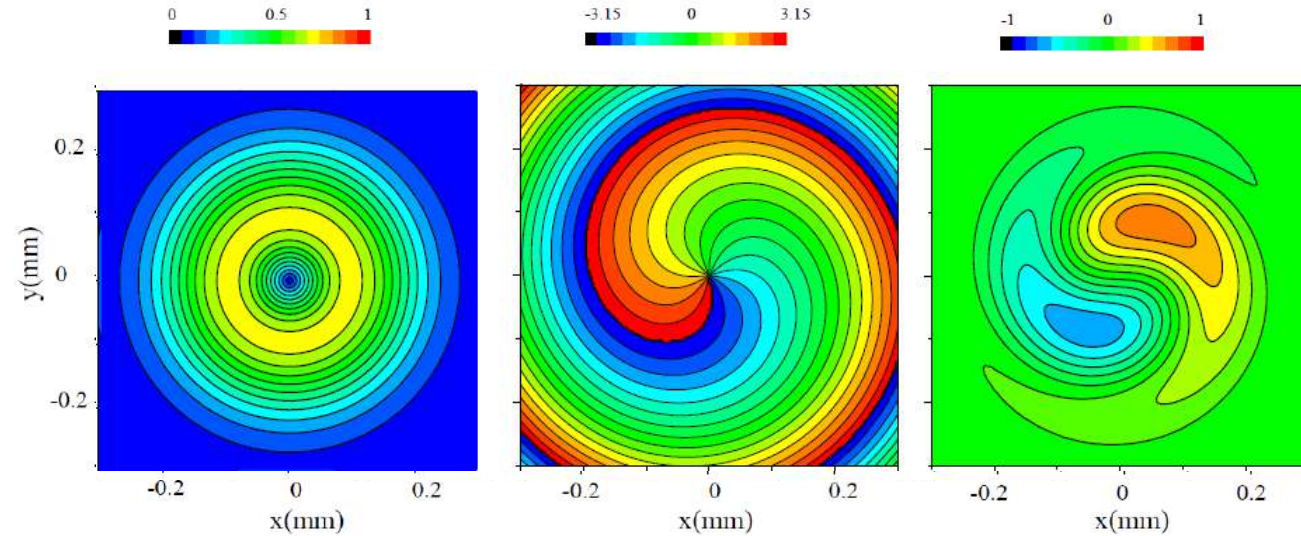
See poster section



Orbital Angular Momentum, radiation calculation

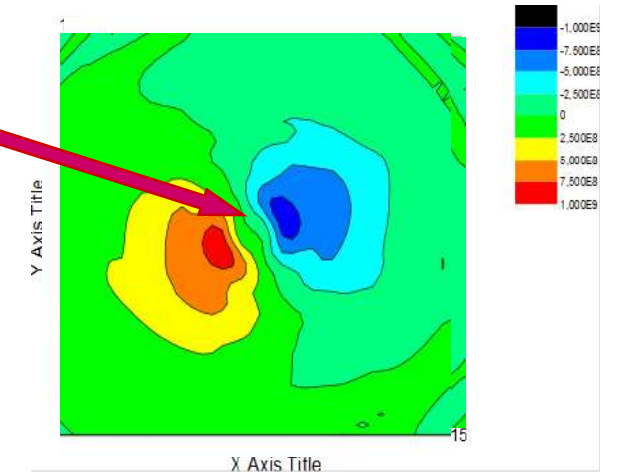
Propagation of the laser:

X radiation the screen,
classical treatment:



vortex

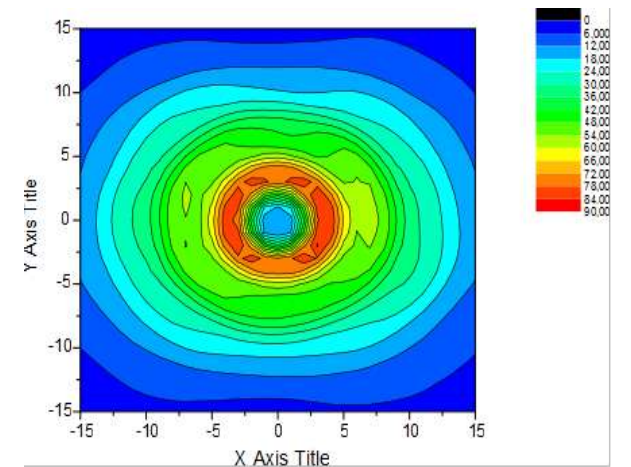
Lienard-Wiechert
electric field:



$$\underline{E} = \frac{e}{c} \sum_j \left[\frac{\underline{n} \times ((\underline{n} - \underline{\beta}_j) \times \dot{\underline{\beta}}_j)}{(1 - \underline{\beta}_j \cdot \underline{n})^3 R} \right]_{ret}$$

$$\dot{\underline{\beta}}_j = -\frac{e}{mc\gamma_j} \left[\underline{E}_L (1 - \underline{\beta}_j \cdot \underline{e}_k) + \underline{\beta}_j \left[\underline{E}_L (\underline{e}_k - \underline{\beta}_j) \right] \right]$$

Quantum treatment:



Generation of High-Energy Photons with
Large Orbital Angular Momentum by Compton Backscattering

U. D. Jentschura^{1,2} and V. G. Serbo^{3,4}

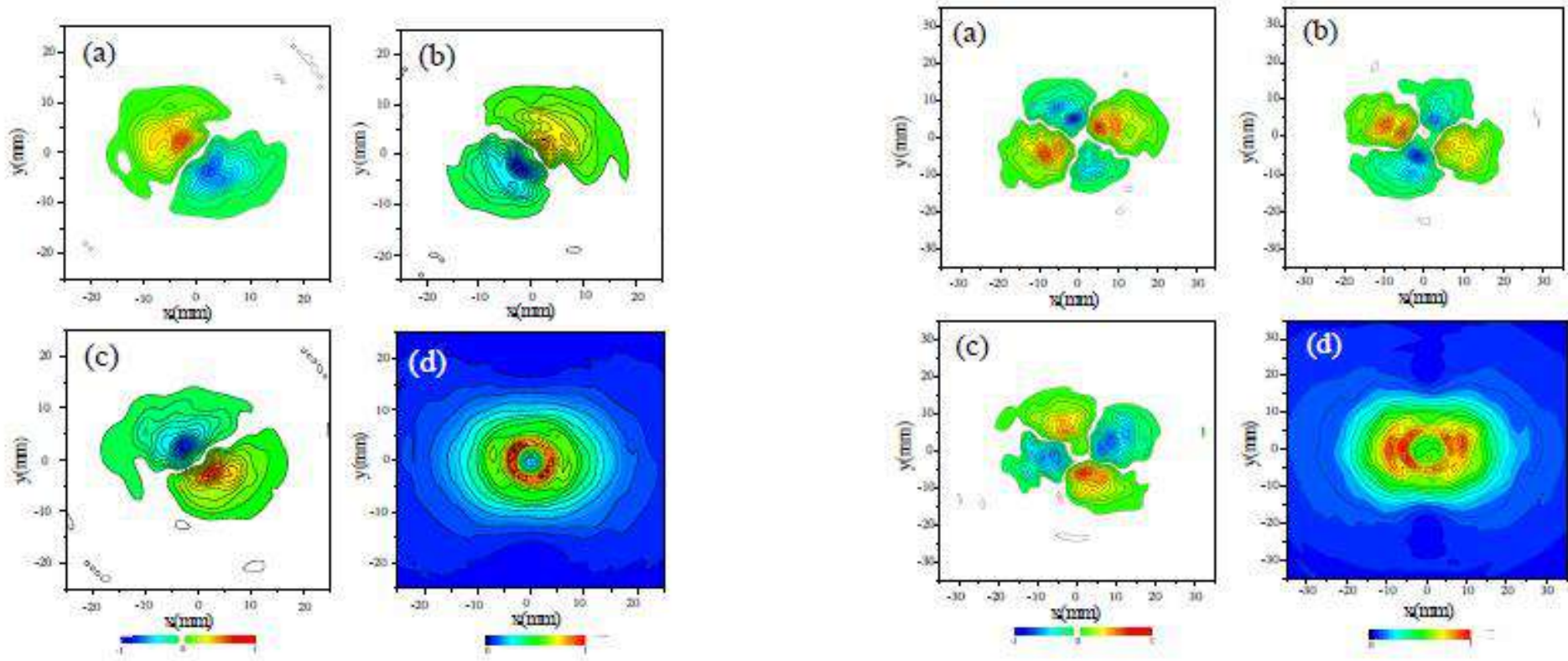
¹Department of Physics, Missouri University of Science and Technology, Rolla, Missouri 65408, USA
²Institut für Theoretische Physik, Universität Heidelberg, Philosophenweg 16, 69120 Heidelberg, Germany
³Novosibirsk State University, Prospekt 2, 630090, Novosibirsk, Russia

scattering of twisted light: angular distribution and polarization of
scattered photons

S. Stock^{1,2}, A. Staudykov¹, S. Fritzsche^{1,2} and D. Sajti^{1,2}

¹Heinrich-Heine-Universität Jena, Fakultät für Physik, 07733 Jena, Germany
²Leibniz-Universität Jena, Theoretisch-Physikalisches Institut, 07733 Jena, Germany

Orbital Angular Momentum, radiation structure

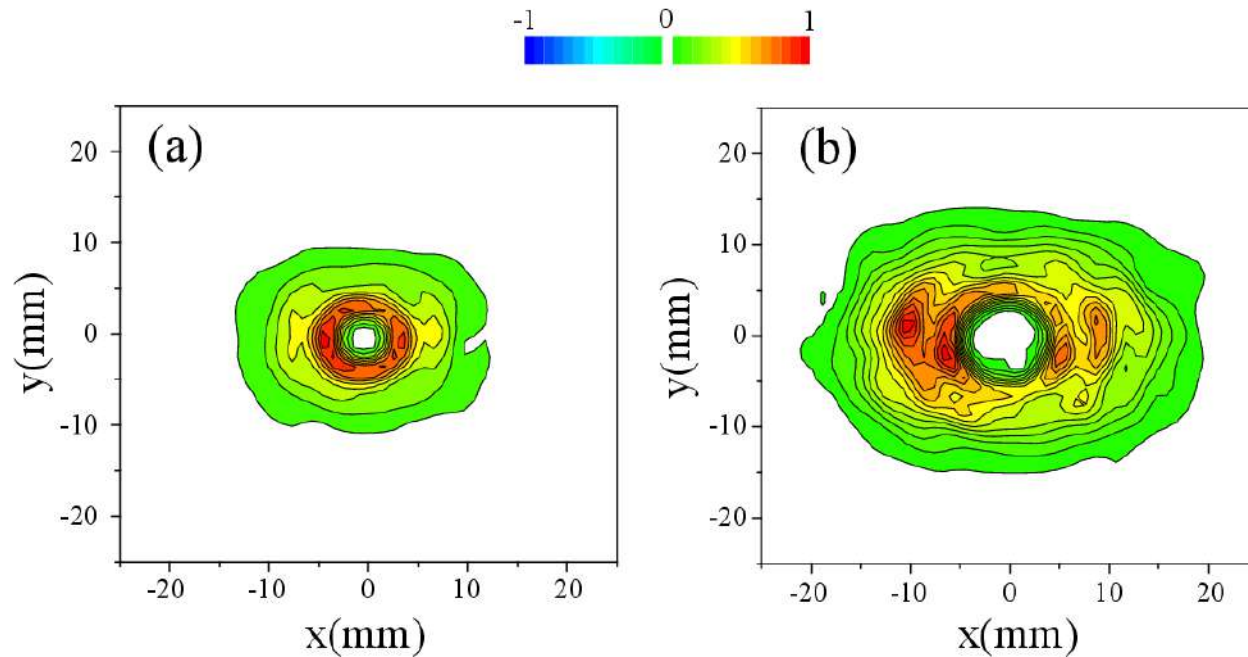


Electric field at different time and averaged intensity on the screen

$m=1$

$m=2$

Orbital Angular Momentum



Orbital Angular Momentum on the screen
 $m=1$ $m=2$

$$N_{\text{ph}} = 6 \cdot 10^6$$
$$E_{\text{ph}} = 8 \text{ keV}$$

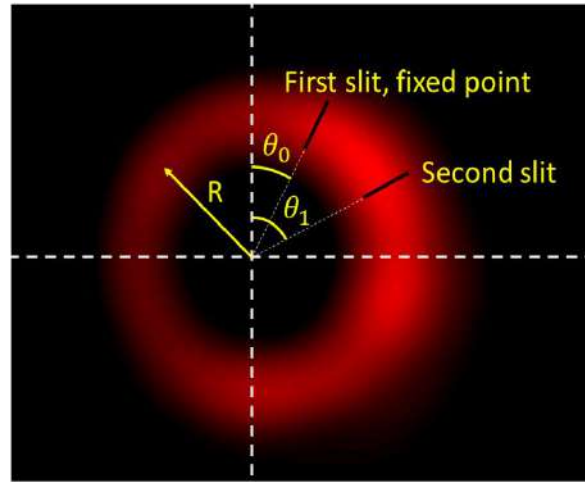
$$\frac{dL_z^{OM,rad}}{dV} \approx \frac{m}{4\pi\omega} |E_y|^2$$

$$L_z^{OM,rad} = 1.7 \times 10^{-27} \text{ J}\cdot\text{s}$$

Electron Energy	25 MeV
Electron Charge	1 nC
Electron Radius	0.1 mm
Electron Length	1 mm
Laser wavelength	800 nm
Laser energy	1 J
Laser waist	0.02 mm
Laser duration	1 ps
Repetition rate	10 Hz

Diagnostics of radiation with Orbital Angular Momentum

DIAGNOSTICS

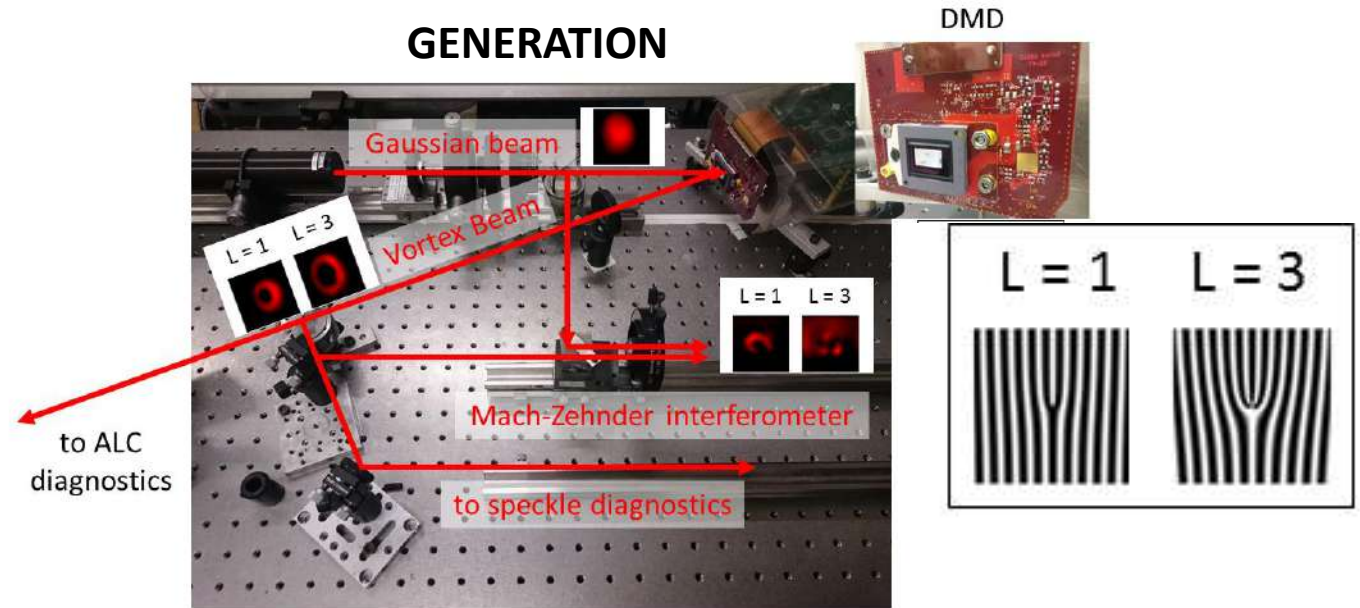


Topological charge and parity are obtained from the **Asymmetric Lateral Coherence (ALC)** of radiation, which is a measurement of the real part of the complex degree of coherence Υ_c with a fixed reference field $E(R, \theta_0)$:

$$\Upsilon_c(R, \theta_0, \theta_1) = \frac{\langle E(R, \theta_0)E^*(R, \theta_1) \rangle}{\mathcal{N}}$$

Azimuthally-arranged pairs of double slits or pinholes allow measurements of the asymmetric lateral coherence.

GENERATION

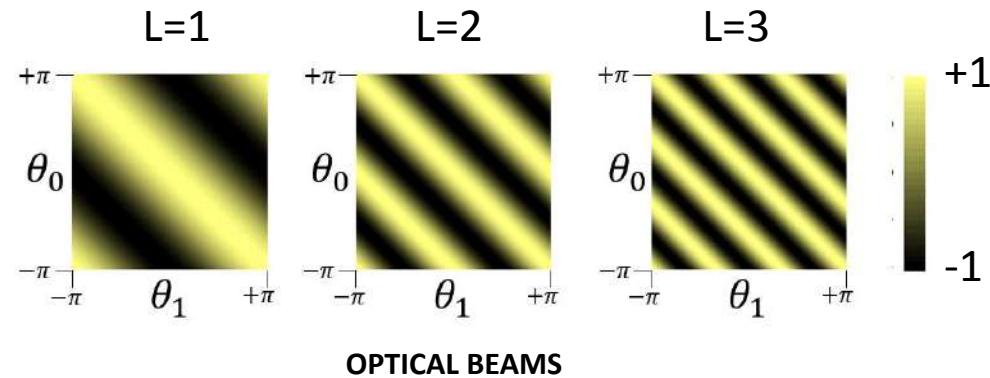


Generation and characterization of optical vortex beams with a Digital Micromirror Device (DMD). Vortices are generated by encoding a corkscrew-like phase modulation on a Gaussian laser beam with computer generated holograms.

Experimental apparatus is used for developments and test of novel diagnostics by scaling from visible light to X-rays.

Simulations of the Asymmetric Lateral Coherence of OAM radiation

- Azimuthal coordinates



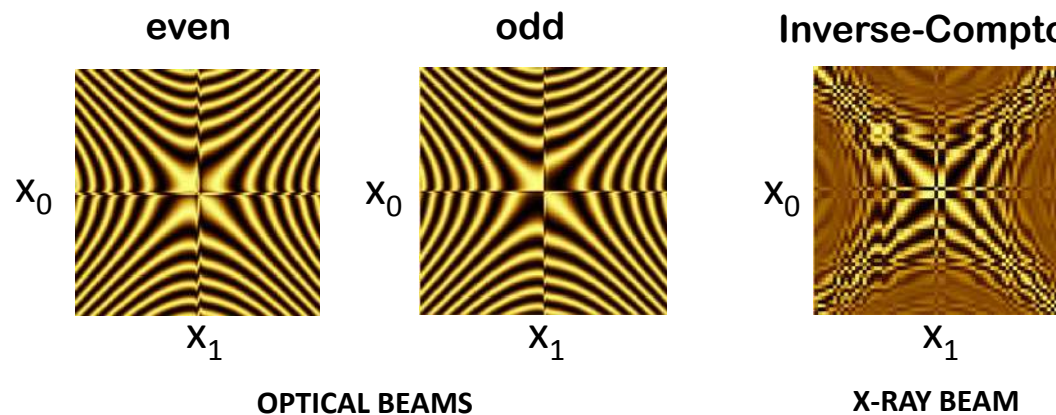
TOPOLOGICAL PROPERTIES:

PARITY

CHARGE

CURVATURE

- Cartesian coordinates



TOPOLOGICAL PROPERTIES:

PARITY

CHARGE

CURVATURE

